Trees

Announcements

Data Abstraction

Data Abstraction

A small set of functions enforce an abstraction barrier between *representation* and *use*

```
• How data are represented (as some underlying list, dictionary, etc.)
```

• How data are manipulated (as whole values with named parts)

E.g., refer to the parts of a line (affine function) called f:

```
•slope(f) instead of f[0] or f['slope']
```

•y_intercept(f) instead of f[1] or f['y_intercept']

Why? Code becomes easier to read & revise; later you could represent a line f as a Python function or as two points instead of a [slope, intercept] pair without changing code that uses lines.

Trees

Tree Abstraction



Recursive description (wooden trees): A tree has a root label and a list of branches Each branch is a tree A tree with zero branches is called a leaf A tree starts at the root Relative description (family trees): Each location in a tree is called a node Each node has a label that can be any value One node can be the parent/child of another The top node is the root node

People often refer to labels by their locations: "each parent is the sum of its children"

Using the Tree Abstraction

For a tree t, you can only:

•Get the label for the root of the tree: label(t)

•Get the list of branches for the tree: branches(t)

•Get the branch at index i, which is a tree: branches(t)[i]

•Determine whether the tree is a leaf: is_leaf(t)

•Treat t as a value: return t, f(t), [t], s = t, etc.

(Demo)

Implementing the Tree Abstraction

```
def tree(label, branches=[]):
    return [label] + branches

def label(tree):
    return tree[0]

def branches(tree):
    return tree[1:]
```



Implementing the Tree Abstraction



Tree Processing

Tree Processing Uses Recursion

```
Processing a leaf is often the base case of a tree processing function
```

The recursive case typically makes a recursive call on each branch, then aggregates

```
def count_leaves(t):
    """Count the leaves of a tree."""
    if is_leaf(t):
        return 1
    else:
        branch_counts = [count_leaves(b) for b in branches(t)]
        return sum(branch_counts)
```

Writing Recursive Functions

Make sure you can answer the following before you start writing code:

- What recursive calls will you make?
- What type of values do they return?
- What do the possible return values mean?
- How can you use those return values to complete your implementation?

Example: Largest Label

```
Processing a leaf is often the base case of a tree processing function
```

The recursive case typically makes a recursive call on each branch, then aggregates

```
def largest_label(t):
    """Return the largest label in tree t."""
    if is_leaf(t):
        return _label(t)
    else:
        return _max([_largest_label(b)_ for b in branches(t)] + [label(t)]_)
```

Example: Largest Label

```
Processing a leaf is often the base case of a tree processing function
```

The recursive case typically makes a recursive call on each branch, then aggregates

```
def above_root(t):
    """Print all the labels of t that are larger than the root label."""
    def process(u):
        if _label(u) > label(t):
            print(_label(u))
        for b in branches(_u):
            process(b)
    process(t)
```