

Data Examples

Announcements

Linked List Construction

Constructing a Linked List

Build the rest of the linked list, then combine it with the first element.



```
s = Link.empty  
s = Link(5, s)  
s = Link(4, s)  
s = Link(3, s)
```

```
def range_link(start, end):  
    """Return a Link containing consecutive  
    integers from start up to end.
```

```
>>> range_link(3, 6)  
Link(3, Link(4, Link(5)))  
"""
```

```
if start >= end:  
    return Link.empty  
else:  
    return Link(start, range_link(start + 1, end))
```

```
def range_link(start, end):  
    """Return a Link containing consecutive  
    integers from start to end.
```

```
>>> range_link(3, 6)  
Link(3, Link(4, Link(5)))  
"""
```

```
s = Link.empty  
k = end - 1  
while k >= start:  
    s = Link(k, s)  
    k -= 1  
return s
```

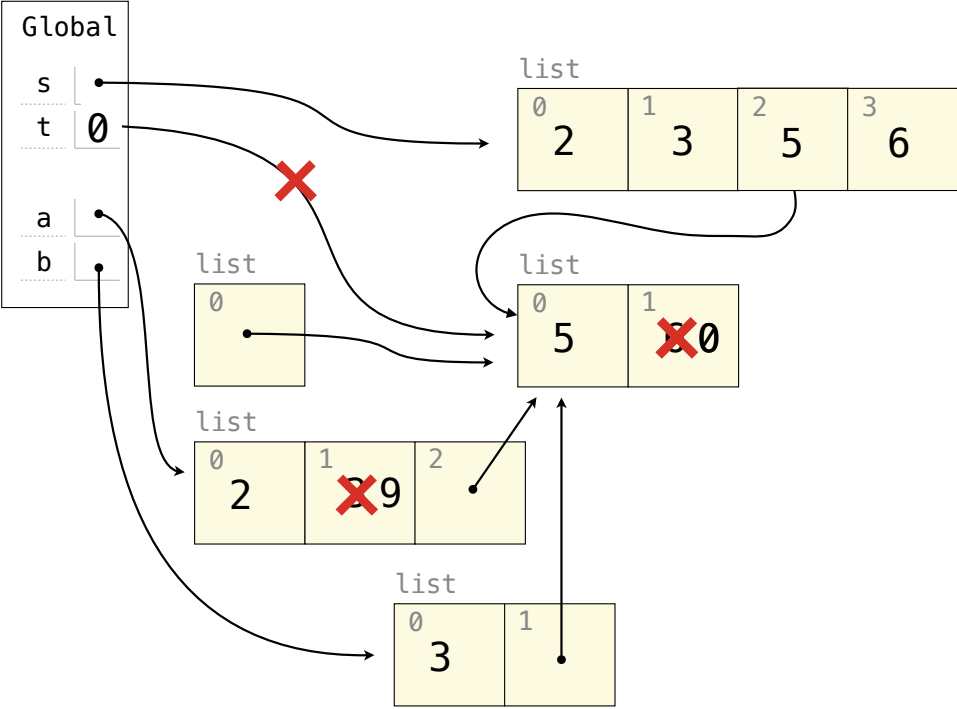
Lists

Lists in Environment Diagrams

Assume that before each example below we execute:

```
s = [2, 3]
t = [5, 6]
```

Operation	Example	Result
append adds one element to a list	s.append(t) t = 0	s → [2, 3, [5, 6]] t → 0
extend adds all elements in one list to another list	s.extend(t) t[1] = 0	s → [2, 3, 5, 6] t → [5, 0]
addition & slicing create new lists containing existing elements	a = s + [t] b = a[1:] a[1] = 9 b[1][1] = 0	s → [2, 3] t → [5, 0] a → [2, 9, [5, 0]] b → [3, [5, 0]]

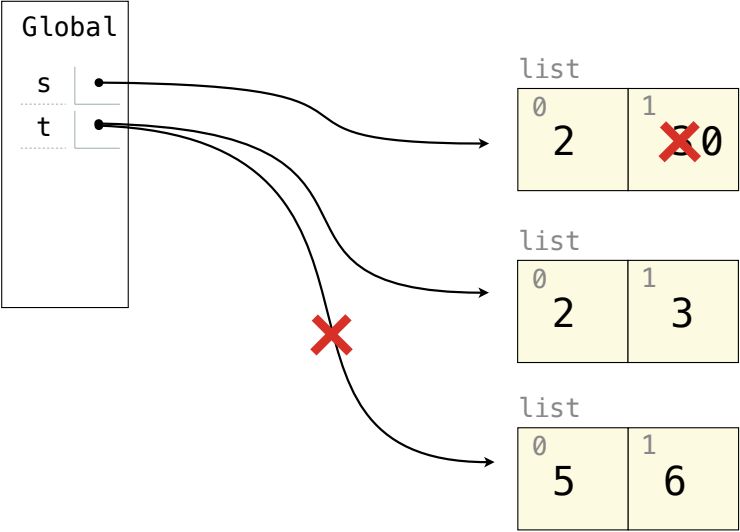


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The list function also creates a new list containing existing elements	t = list(s) s[1] = 0	s → [2, 0] t → [2, 3]



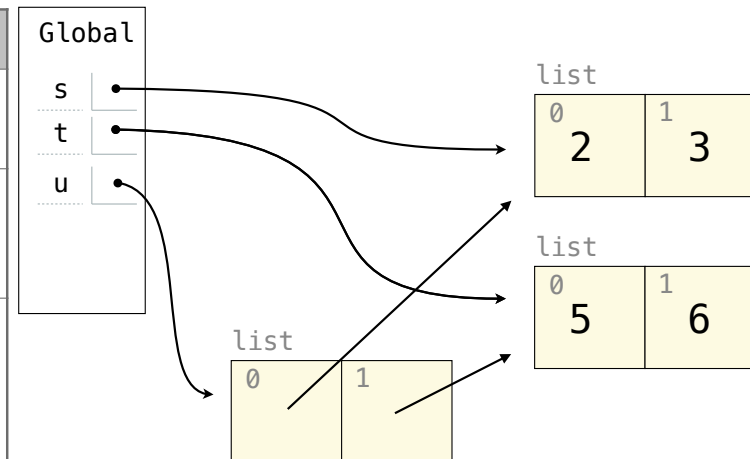
Lists in Environment Diagrams

Assume that before each example below we execute:

`s = [2, 3]`

`t = [5, 6]`

Operation	Example	Result
append adds one element to a list	<code>s.append(t)</code> <code>t = 0</code>	<code>s</code> → [2, 3, [5, 6]] <code>t</code> → 0
extend adds all elements in one list to another list	<code>s.extend(t)</code> <code>t[1] = 0</code>	<code>s</code> → [2, 3, 5, 6] <code>t</code> → [5, 0]
addition & slicing create new lists containing existing elements	<code>a = s + [t]</code> <code>b = a[1:]</code> <code>a[1] = 9</code> <code>b[1][1] = 0</code>	<code>s</code> → [2, 3] <code>t</code> → [5, 0] <code>a</code> → [2, 9, [5, 0]] <code>b</code> → [3, [5, 0]]
The list function also creates a new list containing existing elements	<code>t = list(s)</code> <code>s[1] = 0</code>	<code>s</code> → [2, 0] <code>t</code> → [2, 3]
[...] creates a new list	<code>u = [s, t]</code>	<code>s</code> → [2, 3] <code>t</code> → [5, 6] <code>u</code> → [[2, 3], [5, 6]]



Lists in Environment Diagrams

Assume that before each example below we execute:

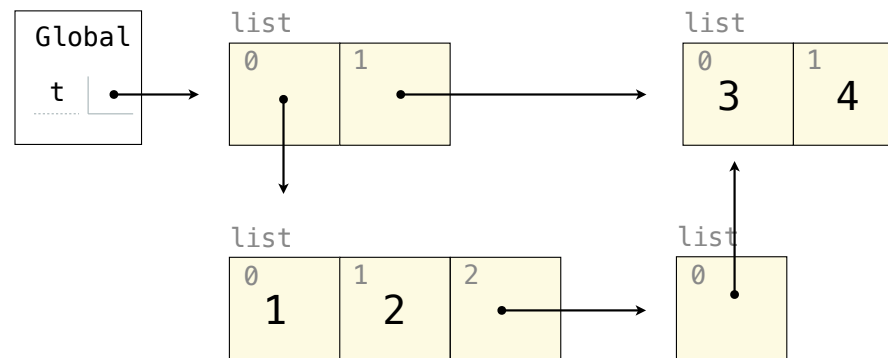
`s = [2, 3]`

`t = [5, 6]`

Operation	Example	Result
pop removes & returns the last element	<code>t = s.pop()</code>	<code>s → [2]</code> <code>t → 3</code>
remove removes the first element equal to the argument	<code>t.extend(t)</code> <code>t.remove(5)</code>	<code>s → [2, 3]</code> <code>t → [6, 5, 6]</code>

Lists in Lists in Lists in Environment Diagrams

```
t = [[1, 2], [3, 4]]  
t[0].append(t[1:2])
```



`[[1, 2, [[3, 4]]], [3, 4]]`

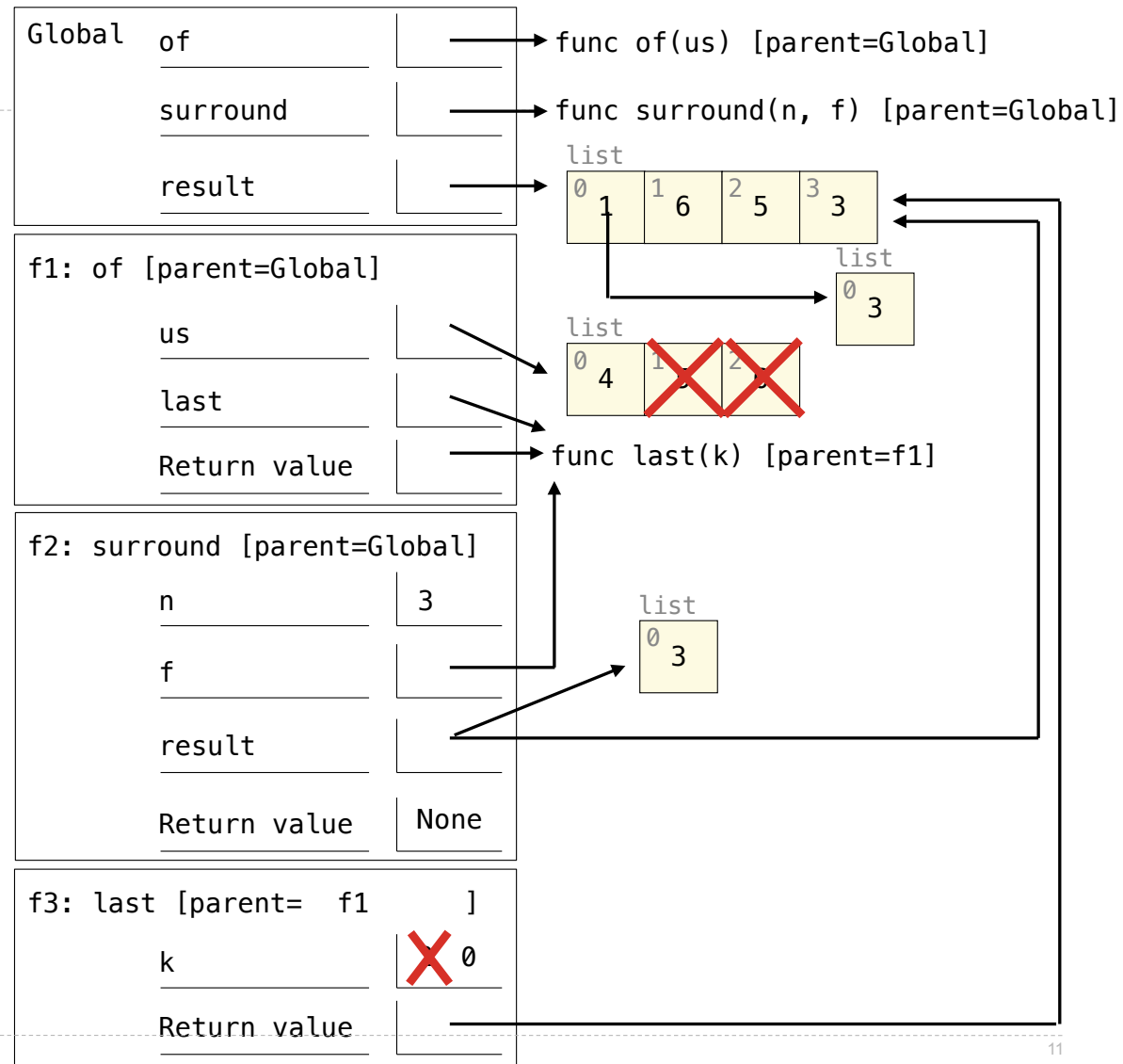
Fall 2022 Midterm 2 Question 2

```
def of(us):
    def last(k):
        "The last k items of us"
        while k > 0:
            result.append(us.pop())
            k = k - 1
        return result
    return last

def surround(n, f):
    "n is the first and last item of f(2)"
    result = [n]
    result = f(2)
    result[0] = [n]
    return result.append(n)

result = [1]
surround(3, of([4, 5, 6]))
print(result)
```

[[3], 6, 5, 3]



Trees



Heracles, Iolaus and the Hydra, Paestan black-figure hydria 6th B.C., [The J. Paul Getty Museum](#)

Fall 2022 Midterm 2 Question 4(b)

A *hydra* is a Tree with a special structure. Each node has 0 or 2 children. All leaves are heads labeled 1. Each non-leaf body node is labeled with the number of leaves among its descendants.

Implement `chop_head(hydra, n)`, which takes a hydra and a positive integer `n`. It mutates hydra by chopping off the `n`th head from the left, which adds two new adjacent heads in its place. Update all ancestor labels.

```
def chop_head(hydra, n):  
    assert n > 0 and n <= hydra.label  
    if hydra.is_leaf():  
        hydra.label = 2  
        hydra.branches = [Tree(1), Tree(1)]  
    else:  
        hydra.label += 1  
        left, right = hydra.branches  
        if n > left.label:  
            chop_head(right, n - left.label)  
        else:  
            chop_head(left, n)
```

