Instructions

Form a small group. Start on problem 1.1. Check off with a staff member or discuss your solution process with a nearby group when you think everyone in your group understands how to solve problem 1.1. Then repeat for 1.2, 1.3, ... You may not move to the next problem until you check off or discuss with another group and everyone understands why the solution is what it is. You may use any course resources at your disposal: the purpose of this review session is to have everyone learning together as a group.
1 Scheme

1.1 What would Scheme display?

(a) > '(1 2 3)
   (1 2 3)

(b) > '(1 . (2 . (3 . ()))))
   (1 2 3)

(c) > '(((1 . 2) . 3) 4 . (5 . 6))
   (((1 . 2) . 3) 4 5 6)

(d) > (cons 1 2)
   (1 . 2)

(e) > (cons 2 '())
   (2)

(f) > (cons 1 (cons 2 '()))
   (1 2)

(g) > (cons 1 (cons 2 3))
   (1 2 . 3)

(h) > (cons (cons (car '(1 2 3)) (list 2 3 4))
     (cons 2 3))
   ((1 2 3 4) 2 . 3)

(i) > (car (cdr (car '((1 2) 3 (4 5))))))
   2

(j) > (cddr '((1 2) 3 (4 5)))
   ((4 5))

1.2 Define sixty-ones. Return the number of times that 1 follows 6 in the list.

> (sixty-ones '(4 6 1 6 0 1))
   1

> (sixty-ones '(1 6 1 4 6 1 6 0 1))
   2

> (sixty-ones '(6 1 6 1 4 6 1 6 0 1))
   3

(define (sixty-ones lst)
  (cond ((or (null? lst) (null? (cdr lst))) 0)
        ((and (= 6 (car lst)) (= 1 (cadr lst))) (+ 1 (sixty-ones (cddr lst))))
        (else (sixty-ones (cdr lst))))))
1.3 Identify the bug(s) in this program.

```
> (sum-every-other '(1 2 3))
4
> (sum-every-other '())
0
> (sum-every-other '(1 2 3 4))
4
> (sum-every-other '(1 2 3 4 5))
9
```

```
(define (sum-every-other lst)
  (cond ((null? lst) lst)
        ((null? (cdr lst)) (car lst))
        (else (+ (car lst)
                  (sum-every-other (cddr lst))))))
```

- The base case should return 0, not `()`. 
- `(cdr lst)` is a list, so it doesn’t make sense to add it to something. Instead, use `(car lst)`, which will give us a number. 
- Using `caar` (first of the first) is incorrect because the first is a number and it doesn’t make sense to get the first of a number. Instead, we should use `cddr` (rest of the rest) to skip forward two elements. However, the `cdr` could be `()`, so we need to add a case to our `cond` to take care of this.

```
(define (sum-every-other lst)
  (cond ((null? lst) 0)
        ((null? (cdr lst)) (car lst))
        (else (+ (car lst)
                  (sum-every-other (cddr lst))))))
```

1.4 (a) Implement add-to-all.

```
> (add-to-all 'foo '((1 2) (3 4) (5 6)))
((foo 1 2) (foo 3 4) (foo 5 6))
```

```
(define (add-to-all item lst)
  (if (null? lst) lst
      (cons (cons item (car lst))
            (add-to-all item (cdr lst))))))
```

(b) Rewrite add-to-all tail-recursively.

```
(define (add-to-all item lst)
  (define (helper item lst added)
    (if (null? lst) added
        (helper item (cdr lst) (append added (list (cons item (car lst)))))))
  (helper item lst '()))
```
1.5 Define sublists. Hint: use add-to-all.

> (sublists '(1 2 3))
(()) (3) (2) (2 3) (1) (1 3) (1 2) (1 2 3)

(define (sublists lst)
  (if (null? lst) '()  
    (let ((recur (sublists (cdr lst))))  
      (append recur (add-to-all (car lst) recur)))))

1.6 (a) Define append. In Scheme, append takes in two lists and returns a larger list.

> (append '(1 2 3) '(4 5 6))
(1 2 3 4 5 6)

(define (append lst1 lst2)  
  (if (null? lst1) lst2  
    (cons (car lst1) (append (cdr lst1) lst2))))

(b) Define reverse. Hint: use append.

> (reverse '(1 2 3))
(3 2 1)

(define (reverse lst)
  (if (null? lst) lst  
    (append (reverse (cdr lst)) (list (car lst)))))

(c) Define reverse tail-recursively. Hint: use a helper function and cons.

(define (reverse lst)
  (define (helper lst reversed)  
    (if (null? lst) reversed  
      (helper (cdr lst) (cons (car lst) reversed ))))
  (helper lst '()))
2 Interpreters

2.1 Circle the number of calls to `scheme_eval` and `scheme_apply` for the code below.

(a) `scm>` `(+ 1 2)`

```
scheme_eval  1  3  4  6
scheme_apply 1  2  3  4
```

4 `scheme_eval`, 1 `scheme_apply`.

(b) `scm>` `(if 1 (+ 2 3) (/ 1 0))`

```
scheme_eval  1  3  4  6
scheme_apply 1  2  3  4
```

6 `scheme_eval`, 1 `scheme_apply`.

(c) `scm>` `(or #f (and (+ 1 2) 'apple) (- 5 2))`

```
scheme_eval  6  8  9  10
scheme_apply 1  2  3  4
```

8 `scheme_eval`, 1 `scheme_apply`.

(d) `scm>` `(define (add x y) (+ x y))`

```
add
scm>` `(add (- 5 3) (or 0 2))`

```
scheme_eval  12  13  14  15
scheme_apply 1  2  3  4
```

13 `scheme_eval`, 3 `scheme_apply`. 
2.2 Identify the number of calls to `scheme_eval` and the number of calls to `scheme_apply`.

(a) `scm> (define pi 3.14)  
    pi  
scm> (define (hack x)  
    (cond  
        ((= x pi) pwned)  
        ((< x 0) (hack pi))  
        (else (hack (- x 1)))))  
    hack 
3 scheme_eval, 0 scheme_apply 

(b) `scm> (hack 3.14)  
    pwned 
9 scheme_eval, 2 scheme_apply 

(c) `scm> ((lambda (x) (hack x)) 0)  
    pwned 
39 scheme_eval, 10 scheme_apply
3 Streams

class Stream:
   """A lazily computed linked list."""

class empty:
   """The empty stream."""

empty = empty()

def __init__(self, first, compute_rest=empty):
   """A stream whose first element is FIRST and whose tail is either a stream or stream-returning parameterless function COMPUTE_REST."""

@property
def rest(self):
   """Return the rest of the stream, computing it if necessary.""

3.1 (a) What are the advantages or disadvantages of using a stream over a linked list?

Lazy evaluation. We only evaluate up to what we need.

(b) What’s the maximum size of a stream?

Infinite

(c) What’s stored in first and rest? What are their types?

first is a value, rest is another stream (either a method to calculate it, or an already calculated stream). In the case of Scheme, this is called a promise.

(d) When is the next element actually calculated?

Only when it’s requested (and hasn’t already been calculated)

3.2 Implement unique_stream which takes in a stream s and returns a new stream that contains only the unique elements of the input stream in the original order. Assume that s is finite.

def unique_stream(s):

    seen = set()

    def compute_rest(s):
        if s is Stream.empty:
            return Stream.empty
        elif s.first in seen:
            return compute_rest(s.rest)
        else:
            seen.add(s.first)
            return Stream(s.first, lambda: compute_rest(s.rest))

    return compute_rest(s)
4  SQL

After more than 100 years of operation, the Ringling Bros. circus is closing. A victory for animal rights advocates, the circus’ closure poses a challenge for the zoologists tasked with moving the circus’ animals to more suitable habitats.

The zoologists must first take the animals in a freight elevator with a weight limit of 2000. In order to speed up the process, the zoologists prefer to take groups of animals of the same species in the elevator, rather than one animal at a time.

Assume the zoologists will only put all of the animals of a particular species in the elevator, or take animals of that particular species one at a time.

You have access to the table animals, with columns containing the animals’ names, weights, and species.

4.1 Write a query that returns the collective weight and species of animals in a group where there is more than one animal of a particular species in a group, and the collective weight of the animals in the group is less than 2000.

Your query should yield the following result.

229 pig
1618 tiger
91 dog

```sql
select sum(weight), species from animals
  group by species having count(*) > 1 and sum(weight) < 2000;
```

4.2 To take the animals to their new habitats, the zoologists load the animals into trucks. The zoologists again want to take the animals in groups of the same species, but one of the trucks has a height limit of 5.0.

Write a query that returns the maximum height and species of animals in a group where the maximum height is less than 5.0. Your query may yield a species where there is only one animal of that particular species.

Your query should yield the following result.

4.1 pig
4 dog
4.9 zebra

```sql
select max(height), species from animals as a, height as b
  where a.name = b.name
  group by species having max(height) < 5.0;
```