2. (14 points) Exercises

(a) (6 pt) Fill in the environment diagram that results from executing the code below until the entire program is finished, an error occurs, or all frames are filled. You may not need to use all of the spaces or frames. A complete answer will:

- Add all missing names and parent annotations to all local frames.
- Add all missing values created or referenced during execution.
- Show the return value for each local frame.

You are not required to write index numbers in list boxes.

```
def f(it):
    it.append(it[1]()()

def b(it):
def steps():
    nonlocal it
    it = fit[0]
    return fit.pop()
    return steps
fit = [1, 2]
bit = [fit, b(fit[1])]
f(bit)
```
(b) (4 pt) Implement `adder`, which takes two lists `x` and `y` of digits representing positive numbers. It mutates `x` to represent the result of adding `x` and `y`. Notes: The built-in `reversed` function takes a sequence and returns its elements in reverse order. Assume that `x[0]` and `y[0]` are both positive.

```python
def adder(x, y):
    """Adds y into x for lists of digits x and y representing positive numbers."

    # 345 + 55 = 400
    >>> a = [3, 4, 5]
    >>> adder(a, [5, 5])
    [4, 0, 0]
    >>> adder(a, [8, 3, 4])  # 400 + 834 = 1234
    [1, 2, 3, 4]
    >>> adder(a, [3, 3, 3, 3])  # 1234 + 33333 = 34567
    [3, 4, 5, 6, 7]
    """
    carry, i = 0, len(x)-1
    for d in reversed([0] + y):
        if ________________________________:
            x.insert(0, 0)
            i = 0
            d = carry + x[i] + d
    if x[0] == 0:
        x.remove(0)
    return x
```

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1. **Lots of Lists**

   Draw the environment diagram that results from executing the following code.

   ```python
   a = [1, 2, 3, 4, 5]
   a.pop(3)
   b = a[:]
   a[1] = b
   b[0] = a[:]
   b.pop()
   b.remove(2)
   c = [1].append(b[1])
   a.insert(b.pop(1), a[3:4:3])
   b.extend(b)
   if b == b[:] and b[1][1][0] is b[0][1][1]:
       a, b, c = [c] + a[4:4:2]
   ```
(e) (8 pt) Implement \texttt{int\_set}, which is a higher-order function that takes a list of non-negative integers called \texttt{contents}. It returns a function that takes a non-negative integer \( n \) and returns whether \( n \) appears in \texttt{contents}. Your partner left you this clue: Every integer can be expressed uniquely as a sum of powers of 2. E.g., 5 equals 1 + 4 equals \texttt{pow(2, 0)} + \texttt{pow(2, 2)}. The \texttt{bits} helper function encodes a list of \texttt{nums} using sequences of 0's and 1's that tell you whether each power of 2 is used, starting with \texttt{pow(2, 0)}.

\textbf{Note:} You may not use built-in tests of list membership, such as an \texttt{in} expression or a list's \texttt{index} method.

\begin{verbatim}
def bits(nums):
    """A set of nums represented as a function that takes 'entry', 0, or 1.
    >>> t = bits([4, 5]) # Contains 4 and 5, but not 2
    >>> t(0)(0)(1)('entry') # 4 = 0 * pow(2, 0) + 0 * pow(2, 1) + 1 * pow(2, 2)
    True
    >>> t(0)(1)('entry') # 2 = 0 * pow(2, 0) + 1 * pow(2, 1)
    False
    >>> t(1)(0)(1)('entry') # 5 = 1 * pow(2, 0) + 0 * pow(2, 1) + 1 * pow(2, 2)
    True
    """
    def branch(last):
        if last == 'entry':
            return 0 in nums
        return ______([______ for k in nums if ________________])
    return branch

def int_set(contents):
    """Return a function that represents a set of non-negative integers.
    >>> int_set([1, 2])(1), int_set([1, 2])(3) # 1 in [1, 2] but 3 is not
    (True, False)
    >>> s = int_set([1, 3, 4, 7, 9])
    >>> [s(k) for k in range(10)]
    [False, True, False, True, False, False, True, False, True, True]
    """
    index = _____________________________________________________________________

def contains(n):
    t = index
    while n:
        last, _______ = __________________________, ______________________
        t = ______________(____________________________)
    return t('entry')

def return contains
5. (13 points) The weakest link

(a) (2 pt) For the following questions, assume that the following generator function is defined:

```python
def naturals():
    i = 1
    while True:
        yield i
        i += 1
```

Implement a generator function called `filter(iterable, fn)` that only yields elements of `iterable` for which `fn` returns `True`.

See the doctests for expected behavior. You may not use the built-in `filter` function or list comprehensions.

Your solution should not require more than 3 lines, and you do not need to use all 3 lines.

```python
def filter(iterable, fn):
    """
    >>> is_even = lambda x: x % 2 == 0
    >>> list(filter(range(5), is_even))
    [0, 2, 4]
    >>> all_odd = (2 * y - 1 for y in range(5))  # Generator object
    >>> list(filter(all_odd, is_even))
    []
    >>> s = filter(naturals(), is_even)
    >>> next(s)
    2
    >>> next(s)
    4
    """

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2. Consistency is Key Fill in the function below so that it conforms to its docstring.

```python
def ensure_consistency(fn):
    """Returns a function that calls fn on its argument, returns fn's
    return value, and returns None if fn's return value is different
    from any of its previous return values for those same argument.
    Also returns None if more than 20 calls are made.
    """

>>> def consistent(x):
    return x

>>> lst = [1, 2, 3]

>>> def inconsistent(x):
    return x + lst.pop()

>>> a = ensure_consistency(consistent)

>>> a(5)
5

>>> a(5)
5

>>> a(6)
6

>>> a(6)
6

>>> b = ensure_consistency(inconsistent)

>>> b(5)
8

>>> b(5)
None

>>> b(6)
7

"""

n =

z =

def helper(x):
    __________
    if __________:
        return __________
    val = fn(x)
    if __________:
        z[x] = [val]
    if __________:
        return __________
    else:
        z[x] = __________
    return __________

return helper