## Instructions

- You have 1 hour to complete the exam.
- The exam is closed book, closed notes, closed computer, closed calculator, except one 8.5” × 11” cheat sheet of your own creation.
- Mark your answers on the exam itself. We will not grade answers written on scratch paper.

<table>
<thead>
<tr>
<th>Last name</th>
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<tbody>
<tr>
<td>First name</td>
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<tr>
<td>Student ID number</td>
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<tr>
<td>Instructional account (cs61a-_)</td>
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<td>BearFacts email (@berkeley.edu)</td>
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<td>Name of the person to your left</td>
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<td>Name of the person to your right</td>
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*All the work on this exam is my own. (please sign)*

1. (10 points) The Ugly Duckling

For each of the expressions in the table below, write the output displayed by the interactive Python interpreter when the expression is evaluated. If an error occurs, write “Error”. If a function is displayed write Function, if a generator is displayed write Generator.

The first box has been filled in for you. Assume that you have started python3 and executed the following statements:

```python
all_ducks = []
class Duck:
    ducks = 0
    def __init__(self, name):
        self.name = name
        all_ducks.append(self)
        Duck.ducks += 1
    def __iter__(self):
        while True:
            yield all_ducks[0]
            first = all_ducks.pop(0)
            all_ducks.append(first)
    def __str__(self):
        return "String Duck"
    def __repr__(self):
        return "Duck(" + self.name + ")"
def clean(self):
    all_ducks = []
    return self
class Duckling:
    mother_duck = Duck
    def __init__(self, name):
        Duck.__init__(self, name)
        self.name = name
    def __repr__(self):
        return "Duckling(" + self.name + ")"
def clean(self):
    all_ducks = []
    return self
class Swan(Duckling):
    def __init__(self, name="autumn"):
        Duckling.__init__(self, name)
        self.mother_duck = self.mother_duck("Swan")
    def __iter__(self):
        return next(Duckling.next)
        while True:
            yield next(Duckling.next)
drake = Duckling("drake")
helen = drake.mother_duck("helen")
iter1 = iter(Duck("temp"))

print("hi")
hi
next(iter1)
Duck.all_ducks[0]
next(iter1)
all_ducks
Duck.ducks
next(iter1)
different = Swan()
different.mother_duck.ducks
all_ducks[0]
new_iter = iter(different)
next(new_iter)
clean(different.mother_duck)
next(iter1)
all_ducks
```

<table>
<thead>
<tr>
<th>Expression</th>
<th>Output</th>
</tr>
</thead>
<tbody>
<tr>
<td><code>print(&quot;hi&quot;)</code></td>
<td>hi</td>
</tr>
<tr>
<td><code>next(iter1)</code></td>
<td>Duck.all_ducks[0]</td>
</tr>
<tr>
<td><code>next(iter1)</code></td>
<td>all_ducks</td>
</tr>
<tr>
<td><code>Duck.ducks</code></td>
<td>next(iter1)</td>
</tr>
<tr>
<td><code>different = Swan()</code></td>
<td>all_ducks[0]</td>
</tr>
<tr>
<td><code>different.mother_duck.ducks</code></td>
<td></td>
</tr>
<tr>
<td><code>new_iter = iter(different)</code></td>
<td></td>
</tr>
<tr>
<td><code>next(new_iter)</code></td>
<td>clean(different.mother_duck)</td>
</tr>
<tr>
<td><code>next(iter1)</code></td>
<td>all_ducks</td>
</tr>
</tbody>
</table>
2. (10 points) Lost in Links

Assume linked lists are defined as follows:

class Link:

    empty = ()

    def __init__(self, first, rest=empty):
        assert rest is Link.empty or isinstance(rest, Link)
        self.first = first
        self.rest = rest

Given a linked list and an interval [i, j], reverse all elements contained between the i and j indices, inclusive. Assume the linked list is 1-indexed (first element is denoted as 1), i < j, and the linked list has strictly more than j elements. Mutate the linked list.

def indexReverse(lnk, i, j):
    """
    >>> ll = Link(1, Link(2, Link(3)))
    >>> indexReverse(ll, 1, 2)
    >>> ll
    Link(2, Link(1, Link(3)))
    >>> ll2 = Link(1, Link(2, Link(3, Link(4, Link(5))))))
    >>> indexReverse(ll2, 2, 4)
    >>> ll2
    Link(1, Link(4, Link(3, Link(2, Link(5))))))
    """

dummy = _______________________________
for _ in ______________________________:
    dummy = ______________________________

reverse = Link.empty

cur = _______________________________
for _ in ______________________________:
    next = ______________________________
    cur.rest = ______________________________
    reverse = ______________________________
    cur = ______________________________

dummy = ______________________________
for _ in ______________________________:
    dummy = ______________________________

reverse = ______________________________
for _ in ______________________________:
    next = ______________________________
    cur.rest = ______________________________
    reverse = ______________________________
    cur = ______________________________

------------------------------------------------------------------
------------------------------------------------------------------
------------------------------------------------------------------
3. (10 points) The Forbidden Forest (of Binary Trees)

Recall the implementation of a Tree:

```python
class Tree:
    def __init__(self, label, branches=[]):
        for c in branches:
            assert isinstance(c, Tree)
        self.label = label
        self.branches = branches

    def is_leaf(self):
        return not self.branches
```

A Binary Search Tree is a tree where the left subtree contains only nodes with keys less than the node's keys, and the right subtree contains only nodes with keys greater than the node's keys. Both left and right subtree must also be Binary Search Trees.

```python
class BST:
    empty = ()
    def __init__(self, entry, left=empty, right=empty):
        self.entry = entry
        self.left, self.right = left, right
```

Write a function `is_binary` that takes in a Tree, `tree`, and returns True if `tree` is a Binary Search Tree and False otherwise.

```python
def is_binary(tree):
    if is_leaf(tree):
        return _________________________________
    left = tree.left
    right = tree.right

    if __________________________________________________________________ :
        return _____________________________________________________________
    return __________________________________________________________________
```

Now write a function `insert` that takes in a Binary Search Tree `tree` and value `n` and inserts `n` into the tree. It mutates `tree` and the return value is also a Binary Search Tree.

```python
def insert(tree, n):
    if tree is BST.empty:
        ___________________________
        to_change = tree.left if n < tree.label else tree.right
```

What is the runtime of `is_binary` if there are n nodes in `tree`? What is the runtime of `insert`?
4. (10 points) Perfect Engine!
You are in an apocalyptic society and have been charged with making an n-gen, or a generator that computes all of the n-perfect numbers. However, in this apocalyptic society, built-in AND user-defined Python multiplication is forbidden in any form!
You have a blueprint for building a few n-gins from a natural number generator:

A 2-gen:
1 2 3 4 5 6 7 8 9 ...
1 4 9 16 25 ...

A 3-gen:
1 2 3 4 5 6 7 8 9 ...
1 3 7 12 19 27 ...
1 8 27 ...

Hint: Here is how yield from works. When used inside an iterable yield from will issue each element from another iterable as though it was issued from the first iterable. The following code is equivalent:

```python
def generator1():
    for item in generator2():
        yield item
    # do more things in this generator

def generator1():
    yield from generator2()
    # more things on this generator
```

Now its your job to build the perfect n-gen and power society out of the apocalypse! Good luck!

```python
def nats():
    """
    A generator that yields all natural numbers.
    Might be helpful!
    """
    curr = 0
    while True:
        curr += 1
        yield curr

def create_skip(n, gen):
    if n == 1:
        yield from ___________
    curr, skip = ________, ________
    for elem in _____________:
        if skip == n:
            _____________
        else:
            curr = _____________
            skip = _____________
            yield _____________

def perfect_ngen(n):
    """
    >>> two_gen = perfect_ngen(2)
    >>> next(two_gen)
    1
    >>> next(two_gen)
    4
    >>> next(two_gen)
    9
    >>> three_gen = perfect_ngen(3)
    >>> next(three_gen)
    1
    >>> next(three_gen)
    8
    >>> next(three_gen)
    27
    """
    gen = create_skip(____, _______)
    while ________________:
        n = ________________
        gen = create_skip(____, _______)
        return gen
```