

## Programs as Data

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## Announcements

## Programs as Data

## A Scheme Expression is a Scheme List

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Scheme programs consist of expressions, which can be:

- Primitive expressions: 2 3.3 true + quotient
- Combinations: (quotient 10 2) (not true)

The built-in Scheme list data structure (which is a linked list) can represent combinations

```
scm> (list 'quotient 10 2)
(quotient 10 2)
```

```
scm> (eval (list 'quotient 10 2))
5
```

In such a language, it is straightforward to write a program that writes a program

(Demo)

## Discussion Question: Automatically Simplifying Code

```
scm> (* 1 2 (* 3 (* 4)) (+ 5 (* 6 (* 7 8))))  
8184
```

```
scm> (flatten-nested-* '(* 1 2 (* 3 (* 4)) (+ 5 (* 6 (* 7 8))))  
(* 1 2 3 4 (+ 5 (* 6 7 8)))
```

```
scm> (* 1 2 3 4 (+ 5 (* 6 7 8)))  
8184
```

```
scm> (eval (flatten-nested-* '(* 1 2 (* 3 (* 4)) (+ 5 (* 6 (* 7 8))))))  
8184
```

```
(define (is-*-call expr) (and (list? expr) (equal? '* (car expr)))) ; E.g., (* 3 4)
```

```
(define (flatten-nested-* expr) ; Return an equivalent expression with no nested calls to *
```

```
  (if (not (list? expr)) expr
```

```
      (let ((expr (map flatten-nested-* expr))) ; Now expr is (* 1 2 (* 3 4) (+ 5 (* 6 7 8)))
```

```
        (if (is-*-call expr)
```

```
            (apply append (map (lambda (e) (if (is-*-call e) (cdr e) (list e))) expr))
```

```
            expr))))
```



(\* 3 4)



(+ 5 (\* 6 7 8))

## Discussion Question: Printing Evaluations

Define `print_evals`, which takes a Scheme expression `expr` that contains only numbers, `+`, `*`, `>`, `if` and parentheses. It prints all of the expressions that are evaluated during the evaluation of `expr` and their values. Print in the **order that evaluation completes**.

Assume every `if` expression has three sub-expressions: predicate, consequence, & alternative.

```
scm> (define expr '(* 2 (if (> 2 (+ 1 1)) (+ 3 4) (* 5 6))))  
expr
```

```
scm> (eval expr)
```

```
60
```

```
scm> (print-evals expr)
```

```
* => #[*]
```

```
2 => 2
```

```
> => #[>]
```

```
2 => 2
```

```
+ => #[+]
```

```
1 => 1
```

```
1 => 1
```

```
(+ 1 1) => 2
```

```
(> 2 (+ 1 1)) => #f
```

```
* => #[*]
```

```
5 => 5
```

```
6 => 6
```

```
(* 5 6) => 30
```

```
(if (> 2 (+ 1 1)) (+ 3 4) (* 5 6)) => 30
```

```
(* 2 (if (> 2 (+ 1 1)) (+ 3 4) (* 5 6))) => 60
```

```
(define (print-evals expr)
```

```
  (if (list? expr)
```

```
      (if (equal? (car expr) 'if )
```

```
          (begin
```

```
            (print-evals (car (cdr expr)))
```

```
            (if (eval (car (cdr expr)))
```

```
                (print-evals (car (cdr (cdr expr))))
```

```
                (print-evals (car (cdr (cdr (cdr expr)))))))
```

```
          (map print-evals expr) ) )
```

```
  (print expr '=> (eval expr)))
```

## Quasiquotation

## Quasiquote

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There are two ways to quote an expression

Quote: `'(a b) => (a b)`

Quasiquote: ``(a b) => (a b)`

Parts of a quasiquoted expression can be unquoted with `,` to evaluate sub-expressions

```
(define b 4)
```

Quasiquote: ``(a ,(+ b 1)) => (a 5)`

Quasiquote is particularly convenient for generating Scheme expressions:

```
(define (make-add-lambda n) `(lambda (d) (+ d ,n)))
```

```
(make-add-lambda 2) => (lambda (d) (+ d 2))
```



## Discussion Question: Fact-Exp

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Use quasiquotation to define **fact-expr**, a procedure that takes an integer *n* and returns a nested multiplication **expression** that evaluates to *n factorial*.

```
scm> (fact-expr 5)
(* 5 (* 4 (* 3 (* 2 (* 1 1))))))
```

```
(define (fact-expr n)
  (if (= n 0) 1 `(* _____ ,n _____ ,(fact-expr (- n 1)) _____ )))
```