CS 61A Summer 2025

Mutability, Iterators, Generators

Mutability

There are many built-in methods that we can use to mutate lists. Here are some of the most useful ones:

- append(el): Appends el to the end of the list and returns None.
- extend(lst): Extends the list by concatenating it with lst and returns None.
- remove(el): Removes the first occurence of el from the list and returns None.
- insert(i, el): Inserts el at index i and returns None.
- pop(i): Removes and returns the element at index i. If no index is given, removes and returns the last element in the list.

Let's see these methods in action:

```
>>> 1 = [3, 5, 6]
>>> 1.append(10)
                     # Append 10 to the end of the list
>>> 1
[3, 5, 6, 10]
>>> l.extend([30, 40])
>>> 1
[3, 5, 6, 10, 30, 40]
>>> l.remove(5)
                    # Remove the first occurrence of 5
>>> 1
[3, 6, 10, 30, 40]
>>> 1.insert(2, -2) # Insert -2 at index 2
>>> 1
[3, 6, -2, 10, 30, 40]
>>> l.pop()
                    # Remove and return the last element
40
>>> 1
[3, 6, -2, 10, 30]
>>> 1.pop(2)
                     # Remove and return the element at index 2
-2
>>> 1
[3, 6, 10, 30]
```

Take note of two things:

- The name 1 refers to the same list object during this entire session; it is never reassigned. The reason the output looks different each time we call a method is because the list that 1 evaluates to is being *mutated*.
- The only method here that has a return value is pop! All of the other methods return None.

Q1: Copying Copies

Draw the environment diagram on paper or a tablet (without having the computer draw it for you)! Then, check your work by stepping through the diagram with PythonTutor

```
def chain(g):
   g(True, g)
def add_copy(p, then):
   copy = result
   if p:
      copy.append(1)
      result.append(list(copy))
      return then(not p, add_copy)
   else:
      copy.append(2)
result = [5]
chain(add_copy)
print(result)
```

See the web version of this resource for the environment diagram.

Iterators

An **iterable** is any value that can be iterated through, or gone through one element at a time. One construct that we've used to iterate through an iterable is a for statement:

for elem in iterable:
 # do something

In general, an **iterable** is an object on which calling the built-in **iter** function returns an *iterator*. An **iterator** is an object on which calling the built-in **next** function returns the next value.

For example, a list is an iterable value.

```
>>> s = [1, 2, 3, 4]
>>> next(s)
                  # s is iterable, but not an iterator
TypeError: 'list' object is not an iterator
>>> t = iter(s)
                  # Creates an iterator
>>> t
<list_iterator object ...>
>>> next(t)
                  # Calling next on an iterator
1
>>> next(t)
                  # Calling next on the same iterator
2
>>> next(iter(t)) # Calling iter on an iterator returns itself
3
>>> t2 = iter(s)
>>> next(t2)
                  # Second iterator starts at the beginning of s
1
                  # First iterator is unaffected by second iterator
>>> next(t)
4
>>> next(t)
                  # No elements left!
StopIteration
>>> s
                  # Original iterable is unaffected
[1, 2, 3, 4]
```

You can also use an iterator in a **for** statement because all iterators are iterable. But note that since iterators keep their state, they're only good to iterate through an iterable once:

```
>>> t = iter([4, 3, 2, 1])
>>> for e in t:
... print(e)
4
3
2
1
>>> for e in t:
... print(e)
```

There are built-in functions that return iterators. These built-in Python sequence operations are said to compute results lazily.

```
>>> m = map(lambda x: x * x, [3, 4, 5])
>>> next(m)
9
>>> next(m)
16
>>> f = filter(lambda x: x > 3, [3, 4, 5])
>>> next(f)
4
>>> next(f)
5
>>> z = zip([30, 40, 50], [3, 4, 5])
>>> next(z)
(30, 3)
>>> next(z)
(40, 4)
```

Q2: WWPD: Iterators

What would Python display?

>>> s = "cs61a"
>>> s_iter = iter(s)
>>> next(s_iter)

>>> next(s_iter)

>>> list(s_iter)

>>> s = [[1, 2, 3, 4]]
>>> i = iter(s)
>>> j = iter(next(i))
>>> next(j)

>>> s.append(5) >>> next(i)

>>> next(j)

>>> **list**(j)

>>> next(i)

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Q3: Repeated

Implement repeated, which takes in an iterator t and an integer k greater than 1. It returns the first value in t that appears k times in a row.

Important: Call **next** on **t** only the minimum number of times required. Assume that there is an element of **t** repeated at least **k** times in a row.

Hint: If you are receiving a **StopIteration** exception, your **repeated** function is calling **next** too many times.

```
def repeated(t, k):
   """Return the first value in iterator t that appears k times in a row,
   calling next on t as few times as possible.
   >>> s = iter([10, 9, 10, 9, 9, 10, 8, 8, 8, 7])
   >>> repeated(s, 2)
   9
   >>> t = iter([10, 9, 10, 9, 9, 10, 8, 8, 8, 7])
   >>> repeated(t, 3)
   8
   >>> u = iter([3, 2, 2, 2, 1, 2, 1, 4, 4, 5, 5, 5])
   >>> repeated(u, 3)
   2
   >>> repeated(u, 3)
   5
   >>> v = iter([4, 1, 6, 6, 7, 7, 8, 8, 2, 2, 2, 5])
   >>> repeated(v, 3)
   2
    0.0.0
   assert k > 1
   "*** YOUR CODE HERE ***"
```

Generators

We can create our own custom iterators by writing a *generator function*, which returns a special type of iterator called a **generator**. Generator functions have **yield** statements within the body of the function instead of **return** statements. Calling a generator function will return a generator object and will *not* execute the body of the function.

For example, let's consider the following generator function:

```
def countdown(n):
    print("Beginning countdown!")
    while n >= 0:
        yield n
        n -= 1
    print("Blastoff!")
```

Calling countdown(k) will return a generator object that counts down from k to 0. Since generators are iterators, we can call iter on the resulting object, which will simply return the same object. Note that the body is not executed at this point; nothing is printed and no numbers are outputted.

```
>>> c = countdown(5)
>>> c
<generator object countdown ...>
>>> c is iter(c)
True
```

So how is the counting done? Again, since generators are iterators, we call **next** on them to get the next element! The first time **next** is called, execution begins at the first line of the function body and continues until the **yield** statement is reached. The result of evaluating the expression in the **yield** statement is returned. The following interactive session continues from the one above.

```
>>> next(c)
Beginning countdown!
5
```

Unlike functions we've seen before in this course, generator functions can remember their state. On any consecutive calls to **next**, execution picks up from the line after the **yield** statement that was previously executed. Like the first call to **next**, execution will continue until the next **yield** statement is reached. Note that because of this, Beginning countdown! doesn't get printed again.

```
>>> next(c)
4
>>> next(c)
3
```

The next 3 calls to **next** will continue to yield consecutive descending integers until 0. On the following call, a **StopIteration** error will be raised because there are no more values to yield (i.e. the end of the function body was

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reached before hitting a yield statement).

>>> next(c)
2
>>> next(c)
1
>>> next(c)
0
>>> next(c)
Blastoff!
StopIteration

Separate calls to **countdown** will create distinct generator objects with their own state. Usually, generators shouldn't restart. If you'd like to reset the sequence, create another generator object by calling the generator function again.

```
>>> c1, c2 = countdown(5), countdown(5)
>>> c1 is c2
False
>>> next(c1)
5
>>> next(c2)
5
```

Here is a summary of the above:

- A generator function has a yield statement and returns a generator object.
- Calling the iter function on a generator object returns the same object without modifying its current state.
- The body of a generator function is not evaluated until **next** is called on a resulting generator object. Calling the **next** function on a generator object computes and returns the next object in its sequence. If the sequence is exhausted, **StopIteration** is raised.
- A generator "remembers" its state for the next next call. Therefore,
 - the first next call works like this:
 - 1. Enter the function and run until the line with yield.
 - 2. Return the value in the yield statement, but remember the state of the function for future next calls.
 - And subsequent next calls work like this:
 - 1. Re-enter the function, start at the line after the yield statement that was previously executed, and run until the next yield statement.
 - 2. Return the value in the yield statement, but remember the state of the function for future **next** calls.
- Calling a generator function returns a brand new generator object (like calling iter on an iterable object).
- A generator should not restart unless it's defined that way. To start over from the first element in a generator, just call the generator function again to create a new generator.

Another useful tool for generators is the yield from statement. yield from will yield all values from an iterator or iterable.

```
>>> def gen_list(lst):
... yield from lst
...
>>> g = gen_list([1, 2, 3, 4])
>>> next(g)
1
>>> next(g)
2
>>> next(g)
3
>>> next(g)
4
>>> next(g)
StopIteration
```

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Q4: Big Fib

This generator function yields all of the Fibonacci numbers.

```
def gen_fib():
    n, add = 0, 1
    while True:
        yield n
        n, add = n + add, n
```

Try to understand the following expression. (It creates a list of the first 10 Fibonacci numbers.)

```
(lambda t: [next(t) for _ in range(10)])(gen_fib())
```

Then, complete the expression below by writing only names and parentheses in the blanks so that it evaluates to the smallest Fibonacci number that is larger than 2024.

```
def gen_fib():
    n, add = 0, 1
    while True:
        yield n
        n, add = n + add, n
    ____(____(lambda n: n > 2024, _____))
```

Q5: Something Different

Implement differences, a generator function that takes t, a non-empty iterator over numbers. It yields the differences between each pair of adjacent values from t. If t iterates over a positive finite number of values n, then differences should yield n-1 times.

```
def differences(t):
    """Yield the differences between adjacent values from iterator t.
    >>> list(differences(iter([5, 2, -100, 103])))
    [-3, -102, 203]
    >>> next(differences(iter([39, 100])))
    61
    """
    "*** YOUR CODE HERE ***"
```

Q6: Primes Generator

Write a function $primes_gen$ that takes a single argument n and yields all prime numbers less than or equal to n in decreasing order. Assume $n \ge 1$. You may use the is_prime function included below, which we implemented in Discussion 1. (The recursive implementation of is_prime is shown here.)

First approach this problem using a for loop and using yield.

```
def is_prime(n):
    """Returns True if n is a prime number and False otherwise.
    >>> is_prime(2)
    True
   >>> is_prime(16)
    False
   >>> is_prime(521)
    True
    .....
    def helper(i):
        if i > (n ** 0.5): # Could replace with i == n
            return True
        elif n % i == 0:
            return False
        return helper(i + 1)
    return helper(2)
def primes_gen(n):
    """Generates primes in decreasing order.
    >>> pg = primes_gen(7)
    >>> list(pg)
    [7, 5, 3, 2]
    .....
    "*** YOUR CODE HERE ***"
```

Now that you've done it using a for loop and yield, try using yield from! Hint: For your base case, remember that 1 isn't a prime.

```
def is_prime(n):
   """Returns True if n is a prime number and False otherwise.
   >>> is_prime(2)
   True
   >>> is_prime(16)
   False
   >>> is_prime(521)
   True
   .....
   def helper(i):
      if i > (n ** 0.5): # Could replace with i == n
         return True
      elif n % i == 0:
         return False
      return helper(i + 1)
   return helper(2)
def primes_gen(n):
   """Generates primes in decreasing order.
   >>> pg = primes_gen(7)
   >>> list(pg)
   [7, 5, 3, 2]
   .....
   if _____:
      return
   if _____:
      yield _____
   yield from _____
```

Q7: Partitions

Tree-recursive generator functions have a similar structure to regular tree-recursive functions. They are useful for iterating over all possibilities. Instead of building a list of results and returning it, just yield each result.

You'll need to identify a *recursive decomposition*: how to express the answer in terms of recursive calls that are simpler. Ask yourself what will be yielded by a recursive call, then how to use those results.

Definition. For positive integers n and m, a *partition* of n using parts up to size m is an addition expression of positive integers up to m in non-decreasing order that sums to n.

Implement partition_gen, a generator functon that takes positive n and m. It yields the partitions of n using parts up to size m as strings.

Reminder: For the partitions function we studied in lecture (video), the recursive decomposition was to enumerate all ways of partitioning n using at least one m and then to enumerate all ways with no m (only m-1 and lower).

Hint: For the base case, yield a partition with just one element, n. Make sure you yield a string.

```
def partition gen(n, m):
    """Yield the partitions of n using parts up to size m.
    >>> for partition in sorted(partition_gen(6, 4)):
            print(partition)
    . . .
    1 + 1 + 1 + 1 + 1 + 1
    1 + 1 + 1 + 1 + 2
    1 + 1 + 1 + 3
    1 + 1 + 2 + 2
    1 + 1 + 4
    1 + 2 + 3
    2 + 2 + 2
    2 + 4
    3 + 3
    .....
    assert n > 0 and m > 0
    if n == m:
        yield ____
    if n - m > 0:
        "*** YOUR CODE HERE ***"
    if m > 1:
        "*** YOUR CODE HERE ***"
```