1 Representation - A Note on Str and Repr

There are two main ways to produce the "string" of an object in Python: `str()` and `repr()`. While the two are similar, they are used for different purposes. `str()` is used to describe the object to the end user in a "Human-readable" form, while `repr()` can be thought of as a "Computer-readable" form mainly used for debugging and development.

When we define a class in Python, `str()` and `repr()` are both built-in functions for the class. We can call an object’s `str()` and `repr()` by using their respective functions. These functions can be invoked by calling `repr(obj)` or `str(obj)` rather than the dot notation format `obj.__repr__()` or `obj.__str__()`. In addition, the `print()` function calls the `str()` function of the object, while simply calling the object in interactive mode calls the `repr()` function.

Here’s an example:

```python
class Test:
    def __str__(self):
        return "str"
    def __repr__(self):
        return "repr"

>>> a = Test()
>>> str(a)
'str'
>>> repr(a)
'repr'
>>> print(a)
str
>>> a
repr
```
Questions

1.1 What would Python display? Feel free to use the environment diagram template below to help with visualization.

class A():
    def __init__(self, x):
        self.x = x
    def __repr__(self):
        return self.x
    def __str__(self):
        return self.x * 2

class B():
    def __init__(self):
        print("boo!")
        self.a = []
    def add_a(self, a):
        self.a.append(a)
    def __repr__(self):
        print(len(self.a))
        ret = ""
        for a in self.a:
            ret += str(a)
        return ret

>>> A("one")

>>> print(A("one"))

>>> repr(A("two"))

>>> b = B()

>>> b.add_a(A("a"))
>>> b.add_a(A("b"))
>>> b
Global frame

f1: [parent=]

Return Value

f2: [parent=]

Return Value

f3: [parent=]

Return Value

Note: This worksheet is a problem bank—most TAs will not cover all the problems in discussion section.
2 Linked Lists

There are many different implementations of sequences in Python. Today, we'll explore the linked list implementation.

A linked list is either an empty linked list, or a Link object containing a first value and the rest of the linked list.

To check if a linked list is an empty linked list, compare it against the class attribute Link.empty:

```python
if link is Link.empty:
    print('This linked list is empty!')
else:
    print('This linked list is not empty!')
```

Implementation

```python
class Link:
    empty = ()
    def __init__(self, first, rest=empty):
        assert rest is Link.empty or isinstance(rest, Link)
        self.first = first
        self.rest = rest

    def __repr__(self):
        if self.rest:
            rest_str = ', ' + repr(self.rest)
        else:
            rest_str = '
        return 'Link({0}{1}).format(repr(self.first), rest_str)

    def __str__(self):
        string = '<'
        while self.rest is not Link.empty:
            string += str(self.first) + ' '  
            self = self.rest
        return string + str(self.first) + '>'
```

Note: This worksheet is a problem bank—most TAs will not cover all the problems in discussion section.
Questions

2.1 Write a function that takes in a linked list and returns the sum of all its elements. You may assume all elements in `lnk` are integers.

```python
def sum_nums(lnk):
    
    >>> a = Link(1, Link(6, Link(7)))
    >>> sum_nums(a)
    14
    ```
Write a function that takes in a Python list of linked lists and multiplies them element-wise. It should return a new linked list.

If not all of the Link objects are of equal length, return a linked list whose length is that of the shortest linked list given. You may assume the Link objects are shallow linked lists, and that \texttt{lst\_of\_lnks} contains at least one linked list.

```python
def multiply_lnks(lst_of_lnks):
    """
    >>> a = Link(2, Link(3, Link(5)))
    >>> b = Link(6, Link(4, Link(2)))
    >>> c = Link(4, Link(1, Link(0, Link(2))))
    >>> p = multiply_lnks([a, b, c])
    >>> p.first
    48
    >>> p.rest.first
    12
    >>> p.rest.rest.rest is Link.empty
    True
    """
    # Note: you might not need all lines in this skeleton code
    ___________ = ___________
    for ________________:
        if ________________:
            _______________
            _______________
            _______________
            _______________
            _______________________
            _______________________
```

Note: This worksheet is a problem bank—most TAs will not cover all the problems in discussion section.
2.3 **Tutorial:** Write a recursive function `flip_two` that takes as input a linked list `lnk` and mutates `lnk` so that every pair is flipped.

```python
def flip_two(lnk):
    """
    >>> one_lnk = Link(1)
    >>> flip_two(one_lnk)
    >>> one_lnk
    Link(1)
    >>> lnk = Link(1, Link(2, Link(3, Link(4, Link(5))))))
    >>> flip_two(lnk)
    >>> lnk
    Link(2, Link(1, Link(4, Link(3, Link(5))))))
    """
```
2.4 Tutorial: Implement `filter_link`, which takes in a linked list `link` and a function `f` and returns a generator which yields the values of `link` for which `f` returns True.

Try to implement this both using a while loop and without using any form of iteration.

```python
def filter_link(link, f):
    """
    >>> link = Link(1, Link(2, Link(3)))
    >>> g = filter_link(link, lambda x: x % 2 == 0)
    >>> next(g)
    2
    >>> next(g)
    StopIteration
    >>> list(filter_link(link, lambda x: x % 2 != 0))
    [1, 3]
    """

    while ________________:
        if ________________:
            ________________
            ________________
```

Note: This worksheet is a problem bank—most TAs will not cover all the problems in discussion section.
3 Trees

Recall the tree abstract data type: a tree is defined as having a label and some branches. Previously, we implemented the tree abstraction using Python lists. Let’s look at another implementation using objects instead:

```python
class Tree:
    def __init__(self, label, branches=[]):
        for b in branches:
            assert isinstance(b, Tree)
        self.label = label
        self.branches = branches

    def is_leaf(self):
        return not self.branches

>>> t = Tree(3, [Tree(4), Tree(5)])
>>> t.label = 5
>>> t.label
5
```

Notice that with this implementation we can mutate a tree using attribute assignment, which wasn’t possible in the previous implementation using lists.

Note: This worksheet is a problem bank—most TAs will not cover all the problems in discussion section.
Questions

3.1 Define a function `make_even` which takes in a tree `t` whose values are integers, and mutates the tree such that all the odd integers are increased by 1 and all the even integers remain the same.

```python
def make_even(t):
    """
    >>> t = Tree(1, [Tree(2, [Tree(3)]), Tree(4), Tree(5)])
    >>> make_even(t)
    >>> t.label
    2
    >>> t.branches[0].branches[0].label
    4
    """
```

3.2 Define a function `square_tree(t)` that squares every value in the non-empty tree `t`. You can assume that every value is a number.

```python
def square_tree(t):
    """Mutates a Tree t by squaring all its elements."""
```
Define the procedure `find_paths` that, given a Tree `t` and an entry, returns a list of lists containing the nodes along each path from the root of `t` to entry. You may return the paths in any order.

For instance, for the following tree `tree_ex`, `find_paths` should return:

```python
def find_paths(t, entry):
    >>> tree_ex = Tree(2, [Tree(7, [Tree(3), Tree(6, [Tree(5), Tree(11)])]), Tree(1, [Tree(5)])])
    >>> find_paths(tree_ex, 5)
    [[2, 7, 6, 5], [2, 1, 5]]
    >>> find_paths(tree_ex, 12)
    []

paths = []
if _________________:
    _____________________________
for _________________:
    ____________________________:
    ____________________________
return ________________
```
3.4 Write a function that combines the values of two trees \( t1 \) and \( t2 \) together with the \texttt{combiner} function. Assume that \( t1 \) and \( t2 \) have identical structure. This function should return a new tree.

Hint: consider using the \texttt{zip()} function, which returns an iterator of tuples where the first items of each iterable object passed in form the first tuple, the second items are paired together and form the second tuple, and so on and so forth.

```python
def combine_tree(t1, t2, combiner):
    """
    >>> a = Tree(1, [Tree(2, [Tree(3)])])
    >>> b = Tree(4, [Tree(5, [Tree(6)])])
    >>> combined = combine_tree(a, b, mul)
    >>> combined.label
    4
    >>> combined.branches[0].label
    10
    """
```

3.5 Implement the \texttt{alt_tree_map} function that, given a function and a \texttt{Tree}, applies the function to all of the data at every other level of the tree, starting at the root.

```python
def alt_tree_map(t, map_fn):
    """
    >>> t = Tree(1, [Tree(2, [Tree(3)]), Tree(4)])
    >>> negate = lambda x: -x
    >>> alt_tree_map(t, negate)
    Tree(-1, [Tree(2, [Tree(-3)]), Tree(4)])
    """
```