INSTRUCTIONS

- You have 2 hours to complete the exam.
- The exam is closed book, closed notes, closed computer, closed calculator, except one hand-written 8.5" × 11" crib sheet of your own creation and the official CS 61A midterm 1 study guide.
- Mark your answers on the exam itself. We will not grade answers written on scratch paper.

<table>
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<tr>
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*All the work on this exam is my own.*

*(please sign)*
1. (10 points) I Wonder What Python Would Display (All are in Scope: WWPD, Higher-Order Functions, Lambda Expressions)

For each of the expressions in the table below, write the output displayed by the interactive Python interpreter when the expression is evaluated. The output may have multiple lines. If an error occurs, write “Error”, but include all output displayed before the error. To display a function value, write “Function”. The first two rows have been provided as examples.

The interactive interpreter displays the value of a successfully evaluated expression, unless it is None.

Assume that you have first started python3 and executed the statements on the left.

<table>
<thead>
<tr>
<th>Expression</th>
<th>Interactive Output</th>
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<tbody>
<tr>
<td>aaron, burr = 2, 5</td>
<td></td>
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<tr>
<td>aaron, burr = 4, aaron + 1</td>
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<tr>
<td>hamil = 10</td>
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</tbody>
</table>
| def alex(hamil):
  def g(w):
    hamil = 2 * w
    print(hamil, w)
    w = hamil
    return hamil
  w = 5
  alex = g(w + 1)
  print(w, alex, hamil) |                     |
| def el(i, za):
  def angelica():
    return i + 1
  if i > 10:
    return za()
  elif i > 4:
    print(angelica())
    return el(i * i, za)
  else:
    return el(i * i, angelica) |                     |
| K = lambda x: lambda y: x |                     |
| def pr(x):
  print(x)
  return x |                     |
2. (8 points) Environmental Influences (All are in Scope: Environment Diagrams, Higher-Order Functions)

Fill in the environment diagram that results from executing the code below until the entire program is finished, an error occurs, or all frames are filled. You may not need to use all of the spaces, frames, or function values.

A complete answer will:

- Add all missing names and parent annotations to all local frames.
- Add all missing values created or referenced during execution.
- Show the return value for each local frame.

```python
x = 1
def f(n):
    def g():
        return n + x
    x = n + 5
    if n % 3 == 0:
        return g
    else:
        return f(n + 1)
x = 10
z = f(2)
q = x + z()
```

<table>
<thead>
<tr>
<th>Line</th>
<th>Code</th>
<th>Global frame</th>
<th>Local frame 1 (f1)</th>
<th>Local frame 2 (f2)</th>
<th>Local frame 3 (f3)</th>
</tr>
</thead>
<tbody>
<tr>
<td>1</td>
<td>x = 1</td>
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<tr>
<td>2</td>
<td>def f(n):</td>
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<td>10</td>
<td>x = 10</td>
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<td>11</td>
<td>z = f(2)</td>
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<tr>
<td>12</td>
<td>q = x + z()</td>
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3. (3 points) **Triangulate (All are in Scope: Control)**

It's easy to see that in any triangle, each side must be shorter than the sum of the other two. Implement `triangle`, which takes three positive numbers, `a`, `b`, and `c`, and returns whether these three numbers could possibly be the lengths of the three sides of a triangle.

```python
def triangle(a, b, c):
    """Return whether a, b, and c could be the legs of a triangle."

    >>> triangle(3, 4, 5)
    True
    >>> triangle(3, 4, 6)
    True
    >>> triangle(6, 3, 4)
    True
    >>> triangle(3, 6, 4)
    True
    >>> triangle(9, 2, 2)
    False
    >>> triangle(2, 4, 2)
    False
    """

    longest = ____________________________

    sum_of_others = ____________________________

    return longest ____________________________ sum_of_others
```
4. (9 points) Digital

(a) (3 pt) (All are in Scope: Recursion) Implement collapse, which takes a non-negative integer, and returns the result of removing all digits from it that duplicate the digit immediately to their right.

def collapse(n):
    """For non-negative N, the result of removing all digits that are equal to the digit on their right, so that no adjacent digits are the same."

    >>> collapse(1234)
    1234
    >>> collapse(12234441)
    12341
    >>> collapse(0)
    0
    >>> collapse(3)
    3
    >>> collapse(1120000013333)
    12013
    """

    left, last = n // 10, n % 10

    if ____________________________________________________________:
        return last
    elif ____________________________________________________________ == ____________________________________________________________:
        return collapse(__________________________________________________________________)
    else:
        return collapse(___________________________) * 10 + ______________________________
(b) (6 pt) (*All are in Scope: Control, Higher-Order Functions*) Implement `find_pair`, which takes a two-argument function, `p`, as input and returns another function. The returned function takes a non-negative integer `n`; it returns `True` if and only if `p` returns a true value when called on at least one pair of adjacent digits in `n`, and `False` otherwise.

```python
def find_pair(p):
    """Given a two-argument function P, return a function that takes a
    non-negative integer and returns True if and only if two adjacent digits
    in that integer satisfy P (that is, cause P to return a true value).
    >>> z = find_pair(lambda a, b: a == b) # Adjacent equal digits
    >>> z(1313)
    False
    >>> z(12334)
    True
    >>> z = find_pair(lambda a, b: a > b)
    >>> z(1234)
    False
    >>> z(123412)
    True
    >>> find_pair(lambda a, b: a <= b)(9753)
    False
    >>> find_pair(lambda a, b: a == 1)(1) # Only one digit; no pairs.
    False
    """

    def find(n):
        while ____________________________:
            if ____________________________:
                return ____________________________

        else:
            ____________________________ = ____________________________
```

---

```python
>>> def find_pair(p):
"""Given a two-argument function P, return a function that takes a
non-negative integer and returns True if and only if two adjacent digits
in that integer satisfy P (that is, cause P to return a true value).

>>> z = find_pair(lambda a, b: a == b) # Adjacent equal digits
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False
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False
>>> z(123412)
True
>>> find_pair(lambda a, b: a <= b)(9753)
False
>>> find_pair(lambda a, b: a == 1)(1) # Only one digit; no pairs.
False
"""
```
5. (10 points) Please Confirm (All are in Scope: Recursion, Higher-Order Functions)

Definition. A confirming function for a sequence of digits, called a code, takes a single digit as its only argument. If the digit does not match the first (left-most) digit of the code to be confirmed, it returns False. If the digit does match, then the confirming function returns True if the code has only one digit, or another confirming function for the rest of the code if there are more digits to confirm.

(a) (5 pt) Implement confirmer so that when confirmer takes a positive integer code, it returns a confirming function for the digits of that code.

```python
def confirmer(code):
    """Return a confirming function for CODE."

    >>> confirmer(204)(2)(0)(4) # The digits of 204 are 2, then 0, then 4.
    True
    >>> confirmer(204)(2)(0)(0) # The third digit of 204 is not 0.
    False
    >>> confirmer(204)(2)(1)   # The second digit of 204 is not 1.
    False
    >>> confirmer(204)(20)    # The first digit of 204 is not 20.
    False
    """

def confirm1(d, t):
    def result(digit):
        if d == digit:
            return t
        else:
            return False
    return result

def extend(prefix, rest):
    """Return a confirming function that returns REST when given the digits of PREFIX. For example, if c = extend(12, confirmer(34)), then c(1)(2) returns confirmer(34), so that c is a confirming function for 1234."""

    left, last = prefix // 10, prefix % 10

    if ________________________________:
        return ________________________________

    else:

        return ________________________________

    return ________________________________
```

(b) (5 pt) Given a confirming function, one can find the code it confirms, one digit at a time. Implement `decode`, which takes a confirming function \( f \) and returns the code that it confirms.

```python
def decode(f, y=0):
    """Return the code for a confirming function f."

    >>> decode(confirmer(12001))
    12001
    >>> decode(confirmer(56789))
    56789
    """

d = 0

while d < 10:

    x, code = _________________________________ , _________________________________

    if x == True:

        return code

    elif x == False:

        _________________________________

    else:

        _________________________________
```