

Sequences

Announcements

Exam Prep Sections!

Lists

```
[ 'Demo ' ]
```

List Indexing

```
digits = [8, 0, 8, 1]
```

```
Index    0  1  2  3
```

```
Index (negative) -4 -3 -2 -1
```

```
>>> digits[2]  
8
```

```
>>> digits[-1]  
1
```

```
x = [3, 1, [4, 1, [5, 2], 6, 5], 3, 5]
```

Write an expression to get the 2: _____

List Indexing

```
digits = [8, 0, 8, 1]
```

```
Index    0  1  2  3
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Index (negative) -4 -3 -2 -1
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>>> digits[2]  
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x = [3, 1, [4, 1, [5, 2], 6, 5], 3, 5]
```

Write an expression to get the 2: _____

List Indexing

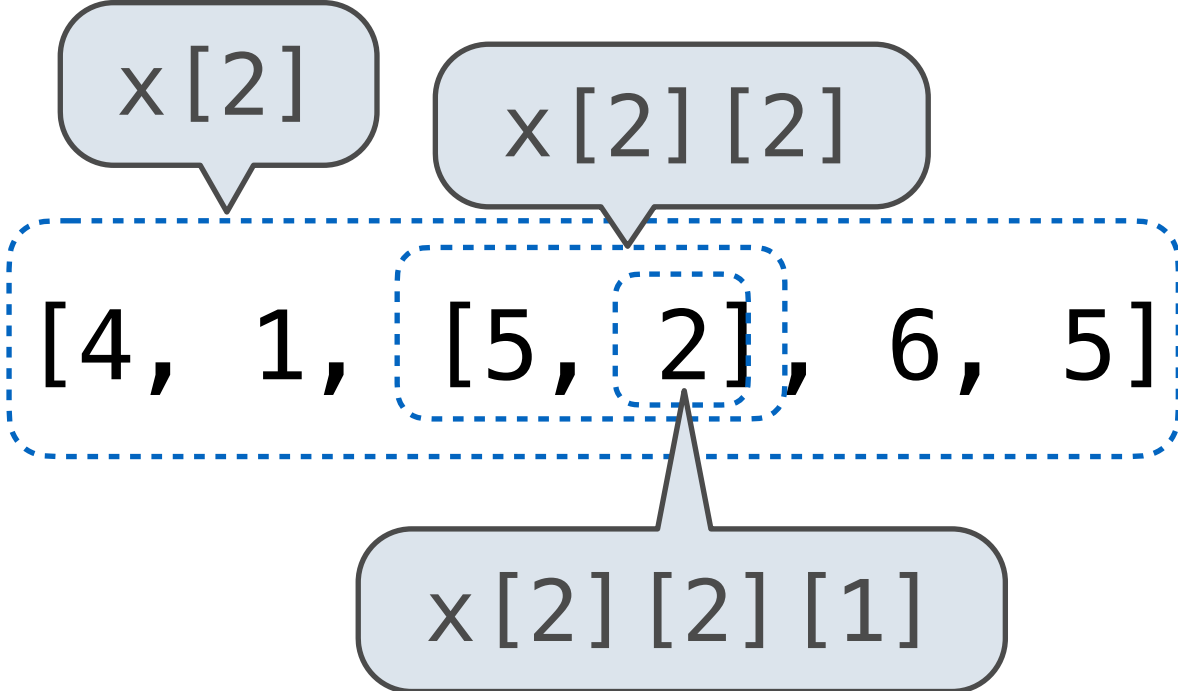
```
digits = [8, 0, 8, 1]
```

```
Index    0  1  2  3
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```
>>> digits[2]  
8
```

```
>>> digits[-1]  
1
```



```
x = [3, 1, [4, 1, [5, 2], 6, 5], 3, 5]
```

Write an expression to get the 2: x[2][2][1]

For Loops

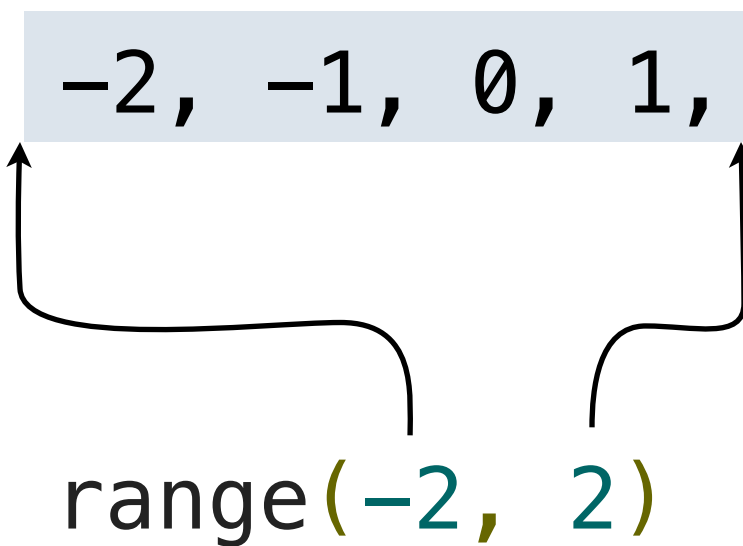
(Demo)

Ranges

The Range Type

A range is a sequence of consecutive integers.*

..., -5, -4, -3, -2, -1, 0, 1, 2, 3, 4, 5, ...



range(-2, 2)

Length: ending value - starting value

(Demo)

Element selection: starting value + index

```
>>> list(range(-2, 2))  
[-2, -1, 0, 1]
```

List constructor

```
>>> list(range(4))  
[0, 1, 2, 3]
```

Range with a 0 starting value

* Ranges can actually represent more general integer sequences.

List Comprehensions

(Demo)

List Comprehensions

A name you choose

```
[<map exp> for <name> in <iter exp> if <filter exp>]
```

Short version: [`<map exp>` `for` `<name>` `in` `<iter exp>`]

Example: Evens

```
def evens(n: int) -> list[int]:  
    """Return a list of the first n even numbers.
```

```
>>> evens(0)  
[]
```

```
>>> evens(3)  
[0, 2, 4]  
"""
```

```
return _____
```

Write down an example!

evens(3):

list(range(3)): [0, 1, 2]

Return value: [0, 2, 4]

Example: Evens

```
def evens(n: int) -> list[int]:  
    """Return a list of the first n even numbers.
```

```
>>> evens(0)  
[]
```

```
>>> evens(3)  
[0, 2, 4]  
"""
```

```
return [2 * x for x in range(n)]
```

Write down an example!

evens(3):

list(range(3)): [0, 1, 2]

Return value: [0, 2, 4]

Example: Promoted

First in Line

Implement **promoted**, which takes a sequence **s** and a one-argument function **f**. It returns a list with the same elements as **s**, but with all elements **e** for which **f(e)** is a true value ordered first. Among those placed first and those placed after, the order stays the same.

```
def promoted(s, f):  
    """Return a list with the same elements as s, but with all  
    elements e for which f(e) is a true value placed first.  
  
    >>> promoted(range(10), odd) # odds in front  
    [1, 3, 5, 7, 9, 0, 2, 4, 6, 8]  
    """  
    return
```

Started with: 0, 1, 2, 3, 4, 5, 6, 7, 8, 9

Result: [1, 3, 5, 7, 9, 0, 2, 4, 6, 8]

Write down an example!

First in Line

Implement **promoted**, which takes a sequence **s** and a one-argument function **f**. It returns a list with the same elements as **s**, but with all elements **e** for which **f(e)** is a true value ordered first. Among those placed first and those placed after, the order stays the same.

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def promoted(s, f):  
    """Return a list with the same elements as s, but with all  
    elements e for which f(e) is a true value placed first.  
  
    >>> promoted(range(10), odd) # odds in front  
    [1, 3, 5, 7, 9, 0, 2, 4, 6, 8]  
    """  
    return [e for e in s if f(e)] + [e for e in s if not f(e)]
```

Started with: 0, 1, 2, 3, 4, 5, 6, 7, 8, 9

Result: [1, 3, 5, 7, 9, 0, 2, 4, 6, 8]

Write down an example!

Lists, Slices, & Recursion

A List is a First Element and the Rest of the List

For any list `s`, the expression `s[1:]` is called a *slice* from index 1 to the end (or 1 onward)

- The value of `s[1:]` is a list whose length is one less than the length of `s`
- It contains all of the elements of `s` except `s[0]`
- Slicing `s` doesn't affect `s`

```
>>> s = [2, 3, 6, 4]
>>> s[1:]
[3, 6, 4]
>>> s
[2, 3, 6, 4]
```

In a list `s`, the first element is `s[0]` and the rest of the elements are `s[1:]`.

Recursion Example: Reverse

```
def reverse(s):  
    """Return s in reverse order.
```

```
>>> reverse([4, 6, 2])  
[2, 6, 4]  
"""
```

```
if not s:  
    return []  
return _____
```

Write down an example!

reverse([4, 6, 2])

What happens if you call the function on everything except the first element?

reverse([6, 2]) + [4]
└──────────┘
[2, 6]

reverse([6, 2])
returns [2, 6]

returns [2, 6, 4]

Recursion Example: Reverse

```
def reverse(s):  
    """Return s in reverse order.  
  
    >>> reverse([4, 6, 2])  
    [2, 6, 4]  
    """  
    if not s:  
        return []  
    return reverse(s[1:]) + [s[0]]
```

Write down an example!

reverse([4, 6, 2])

What happens if you call the function on everything except the first element?

reverse([6, 2]) + [4]
[2, 6]

reverse([6, 2])
returns [2, 6]

returns [2, 6, 4]

Recursion Example: All Possible Sums

```
def sums(n: int) -> list[list[int]]:  
    """Return a list of all of the possible lists of  
    positive integers whose elements add up to n.
```

Write down an example!

```
>>> sums(3)  
[[1, 1, 1], [1, 2], [2, 1], [3]]  
"""
```

```
result = []
```

```
for first in range(1, n):
```

result: []

first: 1

```
    result = result +
```

```
return result + [[n]]
```

Make some return values
where 1 is first?

[[1, 1, 1], [1, 2]]

sums(2): [[1, 1], [2]]

What expression can we write
that results in [1, 1, 1], [1, 2]?

sums(2)

Recursion Example: All Possible Sums

```
def sums(n: int) -> list[list[int]]:
```

```
    """Return a list of all of the possible lists of
    positive integers whose elements add up to n.
```

Write down an example!

```
>>> sums(3)
[[1, 1, 1], [1, 2], [2, 1], [3]]
"""
```

```
result = []
```

```
for first in range(1, n):
```

result: []

first: 1

```
    result = result + [[first] + rest for rest in sums(n - first)]
```

```
return result + [[n]]
```

Make some return values
where 1 is first?

[[1, 1, 1], [1, 2]]

sums(2): [[1, 1], [2]]

What expression can we write [[1] + rest for rest in sums(2)]
that results in [1, 1, 1], [1, 2]?