1 Learning Goals

• Review the basics of environment diagrams and understand them at a deeper level

• Understand the idea of function self-reference as a prelude to recursion (which we will do next week)

• Review higher-order functions and lambda functions at a high level

• Learn how to approach more challenging higher-order function and lambda problems
2 Orientation/Tutorial Review

2.1 Draw the environment diagram that results from executing the code below.

```python
def curry2(h):
    def f(x):
        def g(y):
            return h(x, y)
        return g
    return f
make_adder = curry2(lambda x, y: x + y)
add_three = make_adder(3)
add_four = make_adder(4)
five = add_three(2)
```

Note: This worksheet is a problem bank—most TAs will not cover all the problems in discussion section.
2.2 Write \texttt{curry2} as a lambda function.
2.3 Write a function `print_delayed` that delays printing its argument until the next function call. `print_delayed` takes in an argument `x` and returns a new function `delay_print`. When `delay_print` is called, it prints out `x` and returns another `delay_print`.

```python
def print_delayed(x):
    """Return a new function. This new function, when called, will print out x and return another function with the same behavior."""
    >>> f = print_delayed(1)
    >>> f = f(2)
    1
    >>> f = f(3)
    2
    >>> f = f(4)(5)
    3
    4
    >>> f("hi")
    5
    <function print_delayed> # a function is returned
    ""

def delay_print(y):
    
    return _______________

    return delay_print
```

Note: This worksheet is a problem bank—most TAs will not cover all the problems in discussion section.
3  Additional Practice (Medium-Level Difficulty)

3.1  The following code has been loaded into the Python interpreter:

```python
def skipped(f):
    def g():
        return f
    return g

def composed(f, g):
    def h(x):
        return f(g(x))
    return h

def added(f, g):
    def h(x):
        return f(x) + g(x)
    return h

def square(x):
    return x*x

def two(x):
    return 2
```

What will Python output when the following lines are evaluated?

```
>>> composed(square, two)(7)
```

```
>>> skipped(added(square, two))()(3)
```

```
>>> composed(two, square)(2)
```
4 Exam-Level Practice

4.1 Fall 2020 Midterm 1, Question 3 Fill in each example in the code example below so that its environment diagram is what you see on the following page:

```python
def vote(vote):
    please = ______
    ______ = ty + 3
    return please

ty = 1
register = ______(lambda nov: nov + ty)
________
register(______)
```
HOFs, Lambdas, Self-Reference

Frames

Global frame

Objects

func vote(vote) [parent=Global]
func λ(nov) <line 7> [parent=Global]
func λ(nov) <line 2> [parent=f1]

f1: vote [parent=Global]

vote
please
third
Return value

f2: λ <line 2> [parent=f1]

nov 30
Return value 37

f3: λ <line 7> [parent=Global]

nov 30
Return value 33

Note: This worksheet is a problem bank—most TAs will not cover all the problems in discussion section.